

ORIGINAL RESEARCH PAPER

## The Al<sub>2</sub>O<sub>3</sub>-monolayer sensitivity towards NH<sub>3</sub> and PH<sub>3</sub> molecule: A DFT Study

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### ABSTRACT

The recent theoretical investigation has advocated the Al<sub>2</sub>O<sub>3</sub> monolayer as a stable atomic configuration. This work deals with the interaction of NH<sub>3</sub> and PH<sub>3</sub> towards this monolayer configuration. Structural and electronic investigation suggests a strong affinity of the monolayer towards the NH<sub>3</sub> and PH<sub>3</sub> molecules. PDOS analysis reveals hybridization between the molecular orbital of NH<sub>3</sub>/PH<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub>-monolayer. The electronic energy bandgap of the Al<sub>2</sub>O<sub>3</sub> monolayer gets reduced by 0.26eV and 0.21eV, respectively on NH<sub>3</sub> and PH<sub>3</sub> adsorption. In the band structure analysis of the Al<sub>2</sub>O<sub>3</sub>-monolayer, the energy band dispersion got flattened after the toxic molecular gas (NH<sub>3</sub>/PH<sub>3</sub>) adsorption, suggesting strong sensitivity towards the toxicants. Mulliken population analysis witnessed a robust amount of charge transferred from the toxic molecules to the Al<sub>2</sub>O<sub>3</sub>-nanosheet. A competency in electrical conductivity and energy-band gap flattening of the NH<sub>3</sub>/PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> configurations is an interesting outcome of the present work. All these findings suggest strong sensitivity of the 2D-monolayer for NH<sub>3</sub>/PH<sub>3</sub>.

**Keywords:** DFT, Band structure, Density of State, Mulliken Population Analysis

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### INTRODUCTION

The discovery of graphene is followed by several other novel 2D nanosheets, like boron nitride, silicene, antimonene, arsenene, germanene, etc [1]. These 2D sheets are widely been explored for having interesting electronic, optical, and transport properties [2-9]. At the same time, realizing the extra degree of chemical and physical freedom provided by the nanosurfaces, several groups have explored different molecules' sensitivity towards it both theoretically and experimentally [10-14]. In the race to find a novel 2D-monolayer, recently, Al<sub>2</sub>O<sub>3</sub> nanosheet is predicted and its stability has been confirmed theoretically [15]. Yet the finding is in very infant mode, experimental establishment of the monolayer needs to be investigated. On the other hand, eradicating poisonous gases from the

environment is a need of the hour. To accomplish this aim, the scientific communities have worked on a war footing [16-19]. NH<sub>3</sub> and PH<sub>3</sub> are toxic hazardous molecules that cause severe health effects in the human body. The NH<sub>3</sub> is released into the environment during the production of pesticides, plastics, explosives, dyes, and tyles. The NH<sub>3</sub> harms human bodies by interfering with the normal function of the eyes, throat, and skin. It also consequently decreases the concentration level of oxygen in hemoglobin, hence long-time exposure could be the reason for metabolic activities break down [20-21]. Phosphine in the semiconductor industry works as an agent to introduce phosphorus into silicon crystals. PH<sub>3</sub> is used as an insecticide and pesticide for pollen grains [22]. But its excessive presence in the environment leads to abnormalities in human development. PH<sub>3</sub> attacks the central nervous system and lungs which leads to death. The

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symptom of PH<sub>3</sub> exposure to human health could be nausea, vomiting, abdominal pain, diarrhea, chest pain, etc. The collective observation of the novelty of the Al<sub>2</sub>O<sub>3</sub> nanosheet and the demand for poisonous gas sensors, motivate us to explore the sensitivity of Al<sub>2</sub>O<sub>3</sub> monolayer towards the ammonia (NH<sub>3</sub>) and phosphine (PH<sub>3</sub>) molecules using quantum chemical investigation based on density functional theory (DFT). Previous works have shown dangling lone pairs from NH<sub>3</sub> and PH<sub>3</sub> played an important role in their binding with different nanosurfaces [23, 24]. Thus, any electron-deficient region on the Al<sub>2</sub>O<sub>3</sub> nanosurface could be the NH<sub>3</sub>/PH<sub>3</sub> catcher.

### COMPUTATIONAL METHOD

A 2x2 supercell consisting of 20 atoms (10-Al, 10-O) is employed for ground state calculations. Along the z-axis, a large lattice vector of 20Å is chosen to avoid mirror image interaction. After getting ground state geometry, NH<sub>3</sub> and PH<sub>3</sub>, respectively, are brought near the 2D surface, and allow the configuration to get relaxed within the DFT-based self-consistent field. Interaction with the surface is further explored by investigating structural and electronic changes. All calculations have been performed in the framework of density functional theory (DFT) using Troullier Martins's norm-conserving pseudo-potential [25]. The valence electrons are defined with double zeta double polarized (DZDP) basis set. The exchange-correlation part of hamiltonian has opted for generalized gradient approximation (GGA) in the form of Perdew, Burke, and Ernzerhof (PBE) [26]. An energy cutoff of 250Ry in the real-space grid is employed for numerical integration, and the choice for sampling k-point in the Brillouin zone is 9x9x1 using Monkhorst-Pack scheme [27]. The conjugate gradient algorithm has been used for lattice vectors and atomic position optimization. The Spanish initiative for electronic simulations with thousands of atoms (SIESTA) quantum chemical package [28] is used for all geometrical and structural investigations.

### STRUCTURAL AND ELECTRONIC PROPERTIES

#### Structural Properties

The optimized geometry of Al<sub>2</sub>O<sub>3</sub> is displayed in Fig.1, the in-planner atomic configuration has an average Al-N bond length of 1.69eV as reported before [15]. In the previous report, the stability of

the 2D sheet (or monolayer) is predicted through phonon calculation. Therefore, we are confirmed with the ground state stability of the obtained optimized geometry in the present calculation. The pristine Al<sub>2</sub>O<sub>3</sub> nanosheet has been further exploited to examine the adsorption of NH<sub>3</sub> and PH<sub>3</sub> on its surface, respectively. Al<sub>2</sub>O<sub>3</sub> crystal has an ionic Al-O bonding with Al and O as electron-deficient and electron-rich centers, respectively. We are anticipating a similar bonding pattern in our calculation, hence, expect the electron-rich center of NH<sub>3</sub> and PH<sub>3</sub> to interact with the electron-deficient site (Al) as stated above. The present investigation reveals NH<sub>3</sub> and PH<sub>3</sub> interact with the surface of the Al<sub>2</sub>O<sub>3</sub>-nanosheet through distances of 2.12Å and 2.51Å, respectively. The toxic molecules are directed towards the 2D surface with lone pairs on respective pentavalent atoms (N and P). The closest atoms between the two fragments within NH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> and PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> configuration are N, Al, P, and Al, respectively, as shown in Fig. 2a and 2b. Different orientations of the XH<sub>3</sub> (X = N or P) molecule were relaxed on the Al<sub>2</sub>O<sub>3</sub> monolayer and subsequent findings through formation energy calculation favored the depicted configuration of Fig. 2. Formation energy for NH<sub>3</sub>/PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> is evaluated as

$$E_{\text{Formation}} = E_{\text{XH}_3-\text{Al}_2\text{O}_3} - (E_{\text{Al}_2\text{O}_3} - E_{\text{XH}_3}) \quad (1)$$

$E_{\text{XH}_3-\text{Al}_2\text{O}_3}$ ,  $E_{\text{Al}_2\text{O}_3}$  and  $E_{\text{XH}_3}$  are the total energy of XH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>, Al<sub>2</sub>O<sub>3</sub>-nanosheet and XH<sub>3</sub> molecule, respectively (where, X = N or P). The respective interactions of NH<sub>3</sub> and PH<sub>3</sub> are -1.41eV and -0.70eV, suggesting strong interaction with the monoatomic layer. With these findings, we are confident that a substantial change in an electronic configuration has taken place. This will be explored next through the partial density of state (PDOS) and band structure analysis.

#### Electronic Properties

Energy band structure analysis suggests the Al<sub>2</sub>O<sub>3</sub> monolayer has an energy bandgap of 4.45eV (Fig. 3a), hence falling in the range of wide bandgap semiconductors. It is a direct bandgap semiconductor with conduction band minima (CBM) and valence band maxima (VBM) lying at  $\Gamma$ -point in k-space. A closed look at the energy band dispersion of the Al<sub>2</sub>O<sub>3</sub>-sheet reveals the flattening of energy band spectra after NH<sub>3</sub>/ PH<sub>3</sub> interaction (Fig. 4 a) and (b). As band curvature

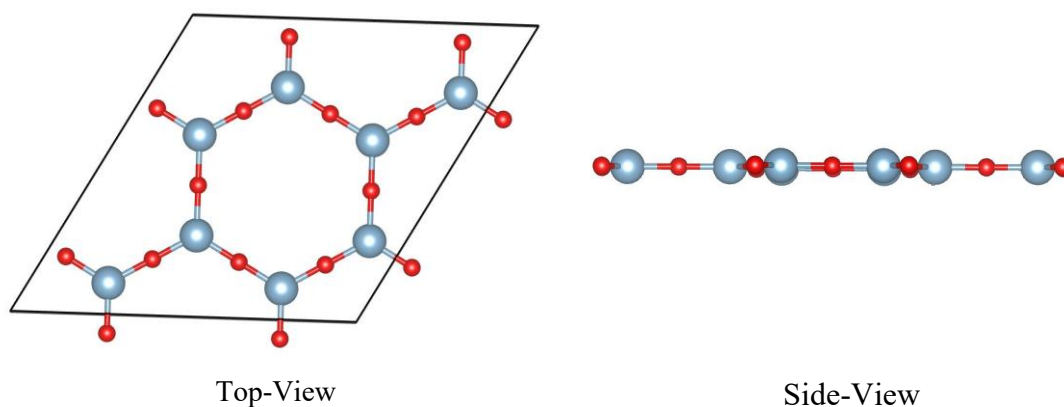


Fig. 1. Optimized ground state geometry of Al<sub>2</sub>O<sub>3</sub> monolayer

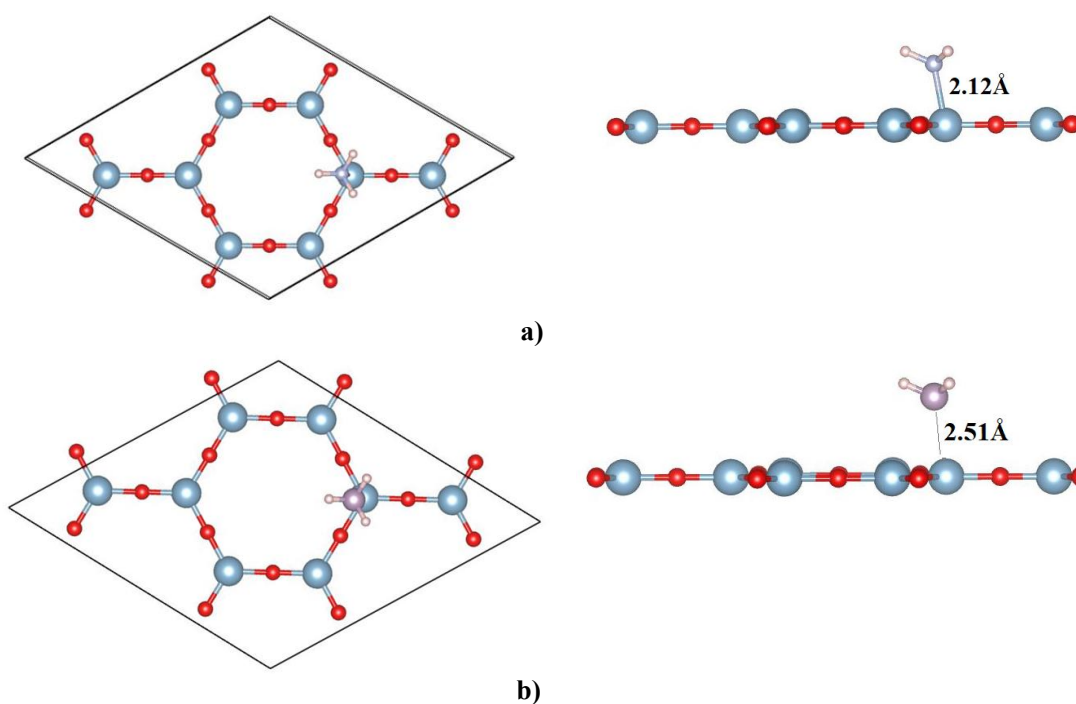


Fig. 2. Top and side-view of a) NH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> and b) PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> atomic configuration.

is inversely proportional to the effective mass of the charge carrier, we expect the charge carrier (electron/hole) mobility of the 2D sheet will become sluggish after NH<sub>3</sub>/ PH<sub>3</sub> adsorption. A slight reduction in the forbidden gap is observed for the molecularly adsorbed 2D sheets. A bandgap of 4.19eV and 4.24eV is witnessed for NH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> and PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> sheets, respectively. The holding of NH<sub>3</sub>/PH<sub>3</sub> over the surface has further been confirmed through electronic charge transfer analysis. Mulliken population analysis identified

a 0.42e charge transferred from NH<sub>3</sub> to the Al<sub>2</sub>O<sub>3</sub> sheet. The charge contribution is mainly attributed to the electronic charge transfer from the lone pair of N to the p-orbitals of Al. A similar pattern is observed for PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> configurations with an electronic charge transfer of 0.33e. In Table.1, we have depicted important electronic and structural parameters to scrutinize the NH<sub>3</sub>/ PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> monolayers. The role of inter-frontier orbital is very important in deciding the chemical behavior of an atomic configuration. In the present investigation,

Table 1. Important parameters for studying the interaction properties of NH<sub>3</sub> and PH<sub>3</sub> on Al<sub>2</sub>O<sub>3</sub>-monolayers.

Configuration	Mulliken Charge Transfer (in e <sup>-</sup> )	Energy gap E <sub>g</sub> (in eV)	NH <sub>3</sub> /PH <sub>3</sub> Distance (from the Al <sub>2</sub> O <sub>3</sub> surface)	Formation energy (in eV) E <sub>Formation</sub>
NH <sub>3</sub> - Al <sub>2</sub> O <sub>3</sub> monolayers	0.42	4.24eV	2.12Å	-1.41eV
PH <sub>3</sub> - Al <sub>2</sub> O <sub>3</sub> monolayers	0.33	4.19eV	2.51Å	-0.70eV

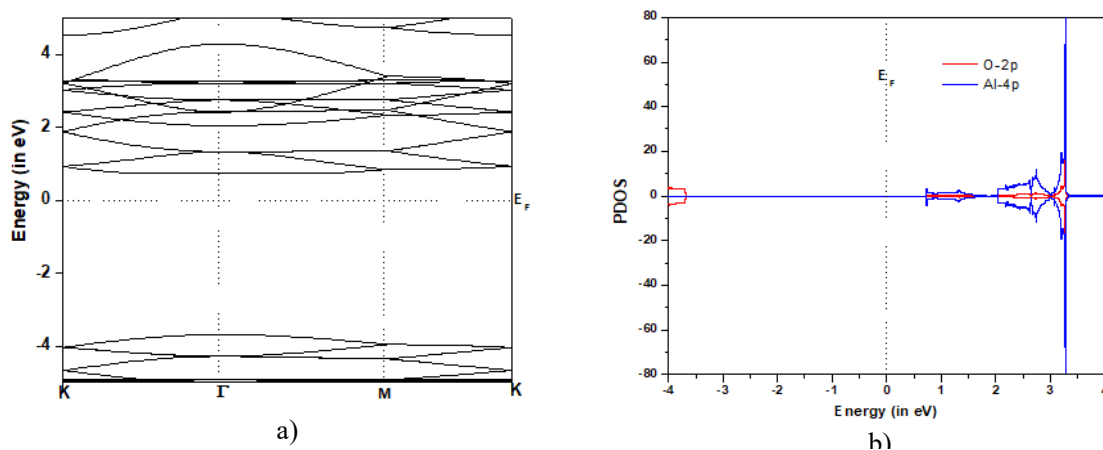


Fig. 3. a) Bandstructure and b) PDOS of pristine Al<sub>2</sub>O<sub>3</sub> nanosheet

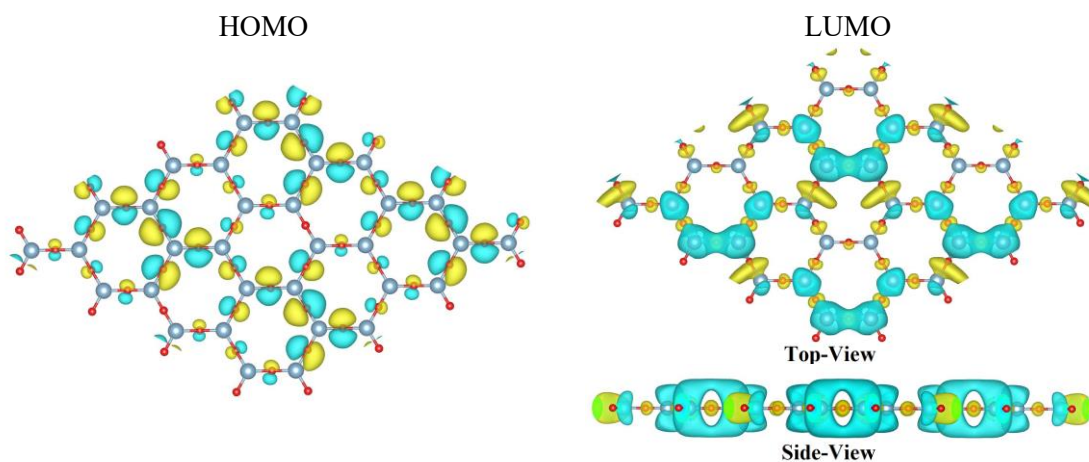


Fig. 4. Contour plot for HOMO and LUMO of the pristine Al<sub>2</sub>O<sub>3</sub> nanosheet

the highest occupied molecular orbital (HOMO) consists of the Al-3p state and the lowest unoccupied molecular orbital (LUMO) is derived from hybridized Al-3p and O-2p state, as evident from the contour plot (Fig. 4). The same is demonstrated in the PDOS plot of pristine Al<sub>2</sub>O<sub>3</sub> (Fig. 3b), no state available is close to the Fermi level. This was also confirmed through band-dispersion analysis in a band structure study. To predict the interaction taking place between NH<sub>3</sub>/PH<sub>3</sub> and the Al<sub>2</sub>O<sub>3</sub>-sheet, fragmented DOS is shown in Fig. 5 (b) and

(d), respectively. The availability of NH<sub>3</sub>/PH<sub>3</sub> and the Al<sub>2</sub>O<sub>3</sub>-DOS at the inter-frontier orbital region (Fig. 3b) and (3d) suggests robust hybridization between molecular orbital from NH<sub>3</sub>/PH<sub>3</sub> and the Al<sub>2</sub>O<sub>3</sub> sheet. The N/P-p<sub>z</sub> orbital gets hybridized with the p<sub>z</sub> orbital of Al which causes it to hold NH<sub>3</sub> and PH<sub>3</sub> over the 2D surface. The conductivity of Al<sub>2</sub>O<sub>3</sub> upon interaction with NH<sub>3</sub>/PH<sub>3</sub> could be

$$\sigma = Ke^{\frac{-E_g}{2K_B T}} \sigma = Ke^{\frac{-E_g}{2K_B T}} \text{ ion} \quad (2)$$

where K is the proportionality constant, E<sub>g</sub> defines

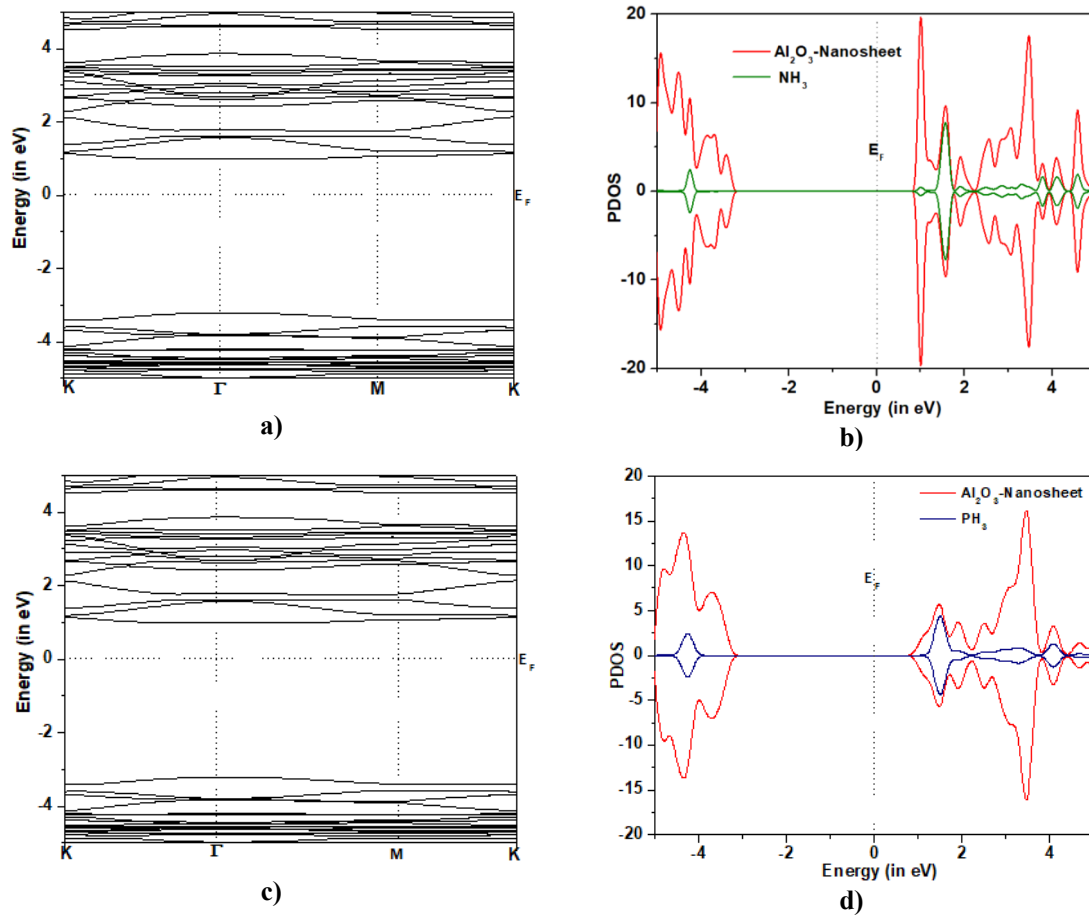


Figure 5. Bandstructure and PDOS of a) NH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> and b) PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>.

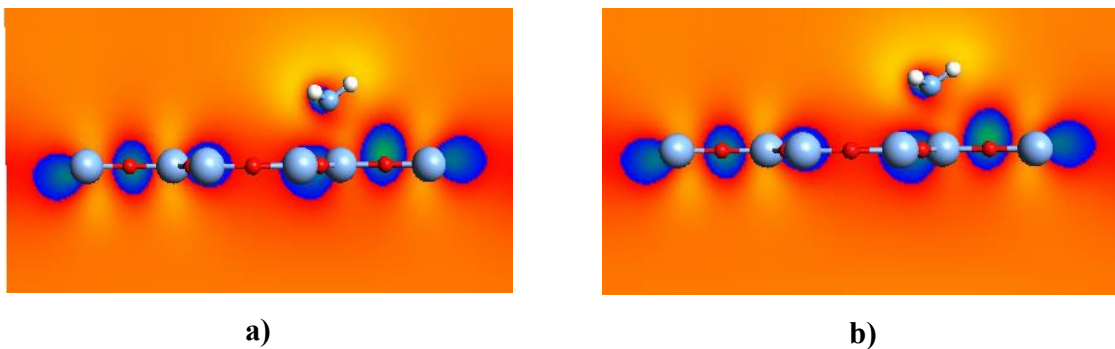


Figure 6. Electrostatic potential difference contour plot of a) NH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> and b) PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> nanosheet.

the energy bandgap,  $K_B$  is the Boltzmann constant and  $T$  is room temperature (300K).

As discussed above, NH<sub>3</sub>/PH<sub>3</sub> interaction  $E_g$  decreased which signifies a rise in electrical conductivity. However, energy band flattening in the band structure diagram suggests increased effective mass of charge carriers, hence, decreased

mobility. Thus, a competing condition is raised to determine the transport behavior of the NH<sub>3</sub>/PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> nanosheet. The depiction of the electrostatic potential difference contour is shown in Fig. 3. The respective dark and light regions signify negative and positive charge accumulation. Relatively, more charge accumulation could be noticed between

NH<sub>3</sub> and the Al<sub>2</sub>O<sub>3</sub> surface compared to the PH<sub>3</sub>. Although the differences are very feeble as mentioned in Mulliken's population analysis, the contour plot depicts a localized charge pattern at O-atoms indicating ionic-bonding character within Al<sub>2</sub>O<sub>3</sub>-monolayer similar to the Al<sub>2</sub>O<sub>3</sub>-matrix.

## CONCLUSIONS

In this work, we investigated the interaction pattern of NH<sub>3</sub>/PH<sub>3</sub> towards the Al<sub>2</sub>O<sub>3</sub>-monolayer. The structural and electronic findings suggest a strong affinity of the toxic molecules towards the 2D nanosheet. With a binding strength of -1.41eV and -0.70eV the molecules were chemisorbed on the 2D surface. The 2D surface holds NH<sub>3</sub>/PH<sub>3</sub> at a distance of 2.12Å/2.51Å with 0.42e/0.33e charges transferred from the latter to the former. The electronic bandgap of the Al<sub>2</sub>O<sub>3</sub>-monolayer gets reduced by 0.26eV and 0.21eV, respectively, on interaction with NH<sub>3</sub> and PH<sub>3</sub>. Envisaging inclusion of the toxic molecular state in the inter-frontier orbital region of the Al<sub>2</sub>O<sub>3</sub>-nanosheet is confirmed in our findings through PDOS analysis. Strong hybridization of lone pair orbital from NH<sub>3</sub>/PH<sub>3</sub> with the valence p-orbitals of O is the reason for electronic charge transfer between the two fragments. The conductivity equation and bandgap flattening indicate delicate competition in deciding charge transport characteristics of the NH<sub>3</sub>/PH<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> configurations.

## CONFLICT OF INTEREST

The authors declare no conflict of interest.

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