Removing Methyl Orange Molecules from Aqueous Medium by Magnetic Nanoparticles: Evaluating adsorption factors, isotherms, kinetics and thermodynamics

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ABSTRACT
In this paper, Fe3O4 and MgFe2O4 as magnetic samples were successfully synthesized by coprecipitation and combustion methods, respectively, to be used for adsorption of toxic methyl orange molecules from the aqueous solution. Characteristics of the synthesized samples were evaluated using various analyses. The results of crystalline and surface bonding assessment confirmed the successful synthesis of both samples with an appropriate structure. Moreover, Fe3O4 presented higher magnetic properties and surface area as well as lower pore diameter than MgFe2O4 sample. However, the maximum adsorption of methyl orange was obtained for MgFe2O4 (56.54 mg/g) which was around three times of Fe3O4 in the same conditions. This may be related to the larger pore diameter of MgFe2O4 and the ease of access to the internal surface of the adsorbent by the adsorbate molecules. Among the evaluated isotherms, the predicted Freundlich model showed a good correlation with the actual results of the adsorption process and the process could kinetically be explained by the pseudo-second-order equation. Thermodynamic investigation of the process showed the adsorption of methyl orange was exothermic and spontaneous. The results revealed that MgFe2O4 sample (qmax = 181.34 mg/g) can be suggested as a good adsorbent for the removal of toxic dyes and water pollutants.

Keywords: Mg-Fe Spinels; Fe3O4; Magnetic Particles; Adsorption; Methyl Orange (MO).

INTRODUCTION
As the most abundant constituent of the human body and the earth is one of the essential substances in the future of humans. Various pollutants such as heavy metals, biological, and dyes are brought into the water from various industries, which can have very devastating effects on human life and the environment. One of the most critical pollutants coming from different industries is waterborne dyes which are produced in industries such as the textile, clothing, dyeing, printing, and food industries [1,2]. These dyes contain toxic and carcinogenic substances that directly affect human health. The importance of these problems has led scientists in recent years to research the possible ways of removing colored substances from water. Chemical methods (dye decomposition), different membranes, and various adsorbents are the most important methods which had been proposed by researchers for removing dyes [3]. Among the methods mentioned, the use of dyes degradation [4] and adsorbents is more attractive for industrial applications due to their convenience and economy [5].
The wide range of adsorbents has been employed in recent years with unique advantages and disadvantages [6]. In most of these studies, the practical factors on adsorption, the proposed isothermal model for the adsorption process (Langmuir, Freundlich, etc.), and the adsorption mechanism have been investigated [7]. For example, Khalil Ibrahim et al. used modified carbon nanotubes to remove methyl orange (MO) dye due to their high thermal and chemical stability [8]. Zayed et al. also used Egyptian Clays to remove MO from the aqueous solution [9]. Moreover, other materials such as silica nanoparticles [10] and zeolite/nickel ferrite/sodium alginate [11] as adsorbents had also been used for eliminating methylene blue dye.

Typical adsorbents used in the adsorption process (such as those mentioned above) have the same problem with difficulty in separation and filtration steps that will increase the cost of the process [12]. Therefore, the magnetic adsorbent can be one of the appropriate methods to overcome this problem to facilitate the adsorbent separation step [13]. Kukarni et al. studied the properties of Fe$_3$O$_4$ fabricated by two routes (co-precipitation and combustion method). They presented that the sample synthesized by the co-precipitation method represented better properties and magnetic activity [14]. In recent years, various mixed material magnetic adsorbents such as activated carbon/ NiFe$_2$O$_4$ [15], lignin-based nanoparticles [16], graphene/magnetite [17], magnetic carbon nanotubes [18], and magnetic carboxylated cellulose [19] have been evaluated in the literature. But, all of the above have complex synthesis steps or costly raw materials and synthesis methods.

Recently, spinels (MgAl$_2$O$_4$, MgFe$_2$O$_4$, CuAl$_2$O$_4$, etc.), which belong to the ceramics family, have been widely used in many industries due to their excellent properties such as chemical and thermal stability and mechanical strength [20]. Various methods for spinel synthesis have been reported in the literature; but, one of the simplest and least expensive ways in this regard is the combustion method [21]. MgFe$_2$O$_4$ were prepared by a facile solvothermal method after 2 days for removing of lead that the maximum adsorption capacity reached to 113.7 mg/g [22]. Lu et al. [23] studied the adsorption capacity of porous MgFe$_2$O$_4$/γ-Fe$_2$O$_3$ magnetic microspheres for the removals of dye (congo red). Although they presented high adsorption capacity for adsorbent, around 2 days consumed for the fabrication of MgFe$_2$O$_4$/γ-Fe$_2$O$_3$, MgFe$_2$O$_4$/biochar magnetic composites also utilized to remove phosphate from aqueous solutions in which the coprecipitation method was used for the preparation of adsorbent. Long and hard synthesis operation under specific conditions was done to obtain the sample after around 3 days [24]. MgFe$_2$O$_4$ modified by (Mn$^{2+}$, Co$^{2+}$, Ni$^{2+}$, and Cu$^{2+}$) has been used for adsorption of methylene blue which the maximum adsorption obtained at catalyst dose of 0.5 g/L and pH of 6.0. The glycine-nitrate method was used for the synthesis of MgFe$_2$O$_4$, which requires much time to obtain the proper adsorbent.

Considering the papers, in which magnetic spinels as adsorbents have been studied, showed that there are no reports of the use of the gel-combustion method in the synthesis of magnetic spinels. Instead of the combustion method, various synthesis methods such as coprecipitation, impregnation, sol-gel, etc. have been reported to synthesize spinels which require too much time and cost [25-27]. On the other hand, it is well known that the synthesis method could have a significant impact on changing spinel specifications [28-30]. However, a lack of study can detect on the spinel materials fabricated by solution combustion method. Moreover, comparing its properties and adsorption ability was not compared in any literature.

Accordingly, in this paper, the magnetic spinel MgFe$_2$O$_4$ was fabricated using a simple and inexpensive combustion method and its physicochemical properties, as well as its ability to be used as the adsorbent of MO, are compared with magnetic Fe$_3$O$_4$ synthesized by co-precipitation method. After choosing the best sample for reducing the concentration of MO from water, the useful parameters for the adsorption as the concentration of dye, adsorbent dosage, pH of the medium, and mixing rate (rpm) were then assessed and the proposed models for kinetics, isotherm, and thermodynamics of the adsorption process were precisely discussed.

**MATERIALS AND METHODS**

**Nano Adsorbents Preparation and Procedure**

For the synthesis of Fe$_3$O$_4$, iron (III) chloride nonahydrate and iron (II) sulfate heptahydrate with the molar ratio of 2 to 1 were stirred in a certain amount of deionized water under nitrogen atmosphere to give a uniform solution.
Subsequently, the NH₄OH aqueous (1.5 M) solution was added dropwise to precipitate the powder until the pH of the solution receives to 10. After ensuring complete deposition (a brown gel), the precipitate was separated by a magnet and washed several times with deionized water until the pH of the washed solution reached 7. Finally, the powder was dried at 50°C for 4 h to form the Fe₃O₄ adsorbent.

For synthesis MgFe₂O₄ adsorbent, iron (III) nitrate nonahydrate, and magnesium nitrate hexahydrate were first dissolved in a desirable amount of deionized water with the molar ratio of 0.5 Mg/Fe. Then, urea fuel was added to the solution at 1.5 times the stoichiometric ratio [21]. After 30 min of stirring on the hot plate at the ambient temperature, the solution temperature was brought to 70°C to form a brown gel by evaporating the water. Then, the brown viscose gel was placed in the oven at 350°C, and after a few minutes, the gel began to combust vigorously. Finally, MgFe₂O₄ brown powder was obtained.

**Nano adsorbents Characterization Techniques**

The Physico-chemical properties of the synthesized adsorbents were determined by X-Ray Diffraction (XRD), Field Emission Scanning Electron Microscopy (FESEM), Surface Particle Size Distribution (SPSD), Vibrating-Sample Magnetometer (VSM), Brunauer-Emmett-Teller (BET)/Barrett-Joyner-Halenda (BJH), Fourier Transform Infrared Spectroscopy (FTIR) and Thermogravimetry (TG) / Differential Thermal Analyser (DTA) analyses were used to investigate. An X’PertPro diffractometer (Holland, Panalytical, Cu Ka: 1.54 angstrom) was used to evaluate the crystalline phases and structure of the samples in the range of 10–80°. The crystalline size of the samples was measured by Scherer’s equation as shown below:

\[ D = \frac{0.9\lambda}{\beta \cos \theta} \]

Where D, \( \lambda \), \( \beta \), and \( \theta \) are crystalline sizes (nm), radiation wavelength (1.5406 Å), corrected half-width of the peak profile and corrected half-width of the diffraction peak angle, respectively.

A MIRA3 FE-SEM device (Czech Republic, TESCAN) was used to assess the surface morphology of the adsorbents. ImageJ software was also used to examine the SPSD of samples. The VSM analysis, which obtained from an MDKB analyzer (Iran, Magnetic Daghigh Kavir), was used to investigate the magnetic strength of the adsorbents. BET-BJH analysis was obtained from a Belsorp mini II analyzer (Japan, Microtrac Bel Corp.). This analysis was used to determine the surface area, pore diameter, and volume of synthesized adsorbents (The degassing of samples was done at 220°C for 3 h). The Spectrum Two analyzer (USA, Perkin Elmer) was used to take FTIR analysis in the 400-4000 cm⁻¹ range using the K-Br tablet method to detection of functional groups belonged to magnetic adsorbents and remained precursors. The TGA also performed by an STA503 instrument (Germany, BAHR) in the range of 30°C to 800°C with a 10°C/min increasing rate and by an argon flow (70 cm³/min).

**Experimental Setup for Adsorption Performance Test**

The methyl orange solution (aq.) was used to investigate the activity of the synthesized adsorbents. For this purpose, the aqueous solution of methyl orange was used at different concentrations (described in the adsorbents efficiency section). In each experiment, specific amounts of adsorbent were added to 50 ml of methyl orange solution to perform the adsorption process. Then, the solution was placed on a shaker to disperse the adsorbent in the methyl orange solution. After the adsorption process was completed, the adsorbent was separated from the solution by a magnet and, then, the centrifuge was used to ensure the complete removal of non-visible absorbent nanoparticles. Finally, UV analysis was used to obtain the amount of methyl orange absorption. A calibration curve of Methyl Orange concentration versus UV absorbance was used to calculate the MO concentration. This curve was prepared by measuring the UV absorbance at 464 nm in an MO concentration region of 5-120 mg/L (Fig. S1). UV analysis was performed by UV-2600 spectrophotometer (Japan, Shimadzu) and each water sample was evaluated three times to ensure the accuracy of the results of each experiment.

**RESULTS AND DISCUSSIONS**

**Assessment the properties of Nano Adsorbents**

**XRD Analysis**

The XRD analysis of the synthesized adsorbents and the standard pattern of the related materials are given in Fig. 1(a). The figure shows that the peaks created for the Fe₃O₄ sample were in perfect agreement with the standard pattern (Cubic, pattern...
Comparing the sample peaks with the standard pattern of Fe$_2$O$_3$ (Rhombohedral, pattern ICDD -01-084-0306) revealed that no Fe$_2$O$_3$ was synthesized during the synthesis of the Fe$_3$O$_4$ sample. By simultaneously evaluating the sample peaks of MgFe$_2$O$_4$ and the reference pattern of MgFe$_2$O$_4$ (Cubic, pattern ICDD-01-073-2211), it can be concluded that the magnetic spinel of MgFe$_2$O$_4$ was correctly synthesized. It observes that the positions of Fe$_3$O$_4$ and MgFe$_2$O$_4$ are the same. It must be mentioned that Fe$_3$O$_4$ and MgFe$_2$O$_4$ have a spinel structure in which the structure was changed from inverse spinel (Fe$_2$O$_3$) to spinel structure (MgFe$_2$O$_4$) by doping Mg cations [31]. Fe$_2$O$_3$ presents the inverse spinel structure in which Fe$^{+2}$ ions occupy the octahedral (B) sites and Fe$^{+3}$ ions occupy both the tetrahedral (A) and octahedral sites ([Fe$^{+3}$]Fe$^{+2}$O$_4$) [19, 35] equally. The inversion parameter decreased with the diffusion of Mg into Fe$_3$O$_4$ lattice. Therefore shifting in the peak positions can detect [32]. Moreover, replacing the Fe cations with Mg cation can affect the positions of peaks due to the difference in the atomic radius of Mg and Fe cations [33].

The MgO (Cubic, ICDD-01-077-2364) was also illustrated in the figure to ensure the synthesis of MgFe$_2$O$_4$ due to the similarity of the standard pattern of the Fe$_2$O$_3$ and MgFe$_2$O$_4$ to each other. It must be mentioned that if the spinel structure was not synthesized, the peak of MgO should be observed in the XRD pattern. The size of the synthesized adsorbent crystals (calculated using the Scherrer equation [34]) is shown in Table 1. The crystalline size of Fe$_3$O$_4$ and MgFe$_2$O$_4$ samples were obtained as 11.9 nm and 7 nm, respectively, indicating that both adsorbents belonged to the nanomaterial family.

**FTIR Analysis**

The FTIR analysis was taken from both samples to investigate the functional groups and their bond type, as shown in Fig. 1(b). Two significant peaks created at 3410 and 1615 cm$^{-1}$ were related to the O-H stretching-bending bonds of the adsorbed water molecules on the surface samples [35]. The peaks at 2830 and 2910 cm$^{-1}$ for MgFe$_2$O$_4$ represented the C-H (stretching-vibration) bonds of urea fuel, which was used in the synthesis process [21]. The presence of these peaks indicated that the fuel did not completely consume during the synthesis process, but, nothing can be said about its value. A large peak created for the MgFe$_2$O$_4$ sample at 1060 cm$^{-1}$ was related to C-N group bonds in urea fuel [36] and, on the other hand, peaks formed at 900, 1390 and 1615 cm$^{-1}$ in the same sample were related to the vibration bonds of NO$_3^-$ group. These peaks indicated the presence of some nitrate in the adsorbents (remaining from the synthesis steps,
which could be determined by TG analysis) [37].
The presence of peaks of 1060 and 1390 cm⁻¹ in
the Fe₃O₄ sample was related to the S = O group
of residual precursors remained from the synthesis
process of this sample [38]. Finally, with peaks in the
range of 400 to 900 cm⁻¹, the synthesis of Fe₃O₄ and
MgFe₂O₄ adsorbents can be assured. It can observe
that only one peak at 460 cm⁻¹ appears for Fe₃O₄,
which could be related to Fe-O bonding while two
peaks detected in 440 cm⁻¹ and 460 cm⁻¹ related to
Mg-O and Fe-O for MgFe₂O₄, respectively [39,37].

**FESEM Analysis**

The FESEM analysis of both synthesized
samples was performed, the results of which are
visible in Fig. 2. The study of both adsorbents
revealed that the samples had nano-dimensions.
Both Fe₃O₄ and MgFe₂O₄ seemed to have the

![FESEM images of Fe₃O₄ and MgFe₂O₄ nano adsorbents: (a) Fe₃O₄, (b) MgFe₂O₄.](image)

**Table 1. Structural properties of Fe₃O₄ and MgFe₂O₄ nano adsorbents.**

<table>
<thead>
<tr>
<th>Nano adsorbent</th>
<th>Synthesis Method</th>
<th>S( BET) (m²/g)</th>
<th>Vₚ (cm³/g)</th>
<th>D (nm)</th>
<th>Crystallite size (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fe₃O₄</td>
<td>Precipitation</td>
<td>80.3</td>
<td>0.375</td>
<td>5.4</td>
<td>11.9</td>
</tr>
<tr>
<td>MgFe₂O₄</td>
<td>Combustion</td>
<td>52.1</td>
<td>0.216</td>
<td>6.9</td>
<td>7</td>
</tr>
</tbody>
</table>

a. Crystallite size estimated by Scherrer’s equation.
b. Crystallite phase: Cubic (JCPDS: 01-077-2364, 2θ = 18.3°, 30.1°, 35.5°, 37.1°, 43.1°, 53.5°, 57.0°, 62.6°, 74.1°, 89.8°)
c. Crystallite phase: Cubic (JCPDS: 01-073-1960, 2θ = 30.2°, 35.6°, 43.2°, 53.6°, 57.2°, 62.8°, 74.3°)
same morphology; however, more uniformity was detected in the structure of the Fe₃O₄ adsorbent. The uniformity could be due to the differences in the synthesis procedures. The sample synthesized by the combustion method due to the uncontrollable nature of the combustion process had more agglomerated particles than the sample synthesized by the co-precipitation method. On the other hand, the use of the combustion method resulted in the formation of more cavities in the MgFe₂O₄ spinel, which might be due to the combustion gases removed from the original gel composition [40]. More porosity with a larger pore diameter caused by the combustion synthesis method can have a noteworthy effect on the absorption of large molecules (such as methyl orange). It makes more accessible the internal surface area of the materials (inside the pores) to dye molecules for easier diffusion/permision [41].

To further investigate the effect of the combustion synthesis method (the MgFe₂O₄ adsorbent was further investigated because of its much better performance in the adsorption process), the FESEM images of MgFe₂O₄ spinel were evaluated using ImageJ software [37] to obtain surface particle size distribution (SPSD). Results of this evaluation, which are mentioned in Fig. 3, showed that the largest and lowest particle sizes in spinel adsorbent were 25.9 and 5.6 nm, respectively, and the average particle size was 14.5 nm. The SPSD also exhibits that the particle size distribution is pointedly in the 10-20 nm range, which was significant for a nano-adsorbent.

VSM Analysis

Magnetic properties of the synthesized samples are one of their important characteristics to provide a simple separation condition after the adsorption of the dyes. For this purpose, VSM analysis was applied as shown in Fig. 4. The saturation magnetic strength for the Fe₃O₄ and MgFe₂O₄ was 48.79 emu/g and 1.79 emu/g, respectively. Due to the presence of Mg in the structure of MgFe₂O₄ decreasing in magnetic strength was predictable. Reduction in the saturation magnetization can be also assigned to the annealing process (combustion process) that it renders domains motion/rotation and leads to higher kinetic energy [42,43].

It is also clear that there was no hysteresis for both samples which is related to a superpara-

![Fig. 3. Surface Particle size distribution histogram of MgFe₂O₄ nano adsorbents.](image-url)
magnetic nature [35]. These materials do not cling to each other (agglomeration) in the absence of a magnetic field because they only have the magnetic properties in the presence of the field, making them easy to use as adsorbents [44].

**BET/BJH Analysis**

One of the most important parameters in the adsorption process is the surface area and pore volume and diameter of the adsorbent. These specifications were obtained for both studied samples by BET-BJH analysis, the results of which are presented in Table 1 and Fig. 5. It can be observed in Table 1 that the specific surface area of Fe₃O₄ was about 1.5 times of the magnetic spinel of MgFe₂O₄. The difference in surface area can be due to the different nature of the two materials as well as the various synthesis methods [21]. Also, by comparing the pore volume and diameters, it is found that the Fe₃O₄ adsorbent had higher pore volume, but lower pore diameter than the magnetic spinel. Due to the large size of the methyl orange molecules, the used adsorbent must have a large pore diameter to allow a better adsorption process. Therefore, the MgFe₂O₄ sample with an average pore diameter of 6.9 nm compared to Fe₃O₄ with the average pore diameter of 5.4 nm can be better adsorbent for coarse methyl orange molecules [45].

It can be observed that both adsorbents fell into category IV of the IUPAC classification for porous materials (that were related to mesopore materials) by examining Fig. 5 and the absorption curves of the two synthesized magnetic samples. The adsorption-desorption hysteresis of both adsorbents was also very similar to the H1 type, which indicated the formation of cylindrical holes in the adsorbents. The created cylindrical pores in the samples can facilitate the entry of large methyl orange molecules into the adsorbent pores and, thus, increase access to the internal adsorbent surface [34]. As seen in Fig. 5, the maximum size distribution of the pore diameters of both adsorbents was in the range of 2
to 30 nm, which proved that the adsorbents were mesopore (2–50 nm).

**TG Analysis**

TG analysis was used to qualitatively evaluate the synthesized adsorbents, the results of which are shown in Fig. 6. The amount of additional material (such as water, precursors, etc.) remained in/on the samples can be evaluated using this analysis. The Fe₃O₄ and MgFe₂O₄ samples showed a 3 and 12% decrease in weight between 30-200°C, respectively. This reduction might be due to the absorption of gases in the atmosphere, such as water and carbon dioxide, onto the surface of the adsorbents. There was also a 3.3% decrease in Fe₃O₄ sample at the temperatures between 200 and 450°C, which could be related to the decomposition of chloride and sulfate compounds in the precursors. In the same temperature range for the MgFe₂O₄ magnetic spinel, a 12% decrease in weight was observed, which was due to the decomposition of the nitrate precursor materials used in the synthesis of this sample. Finally, at temperatures above 450°C, almost no decrease was observed in the Fe₃O₄ sample; but, for the MgFe₂O₄ spinel, a decrease of about 5.3% was achieved, which could be due to the decomposition of urea fuel remaining from the combustion stage in this sample. According to the results, there was a good agreement between the results of FTIR and TG analysis.

**Performance Study toward Removal of Methyl Orange**

**Optimum adsorbent**

Both synthesized adsorbents were investigated under similar conditions in the methyl orange adsorption process from water. For this purpose, 0.05 g of the adsorbent was poured into 50 ml of
methyl orange solution in water (100 mg MO/L) at pH 6. The solution with the adsorbent was placed in a shaker at 200 rpm and the mixing temperature was adjusted to 25°C. After 1 h of the adsorption process, some samples were taken from both test vessels by a syringe containing a filter syringe. To ensure that no adsorbent was present in the sample solution, they were centrifuged at 6000 rpm for 15 min. Then, spectrophotometer analysis in the range of 350 to 600 cm⁻¹ was used to obtain methyl orange absorption.

The results showed that the adsorption amount of MO on the surface of Fe₃O₄ and MgFe₂O₄ adsorbents in the mentioned condition was 20 mg/g and 56.54 mg/g, respectively. Thus, it was found that the MgFe₂O₄ sample had stronger adsorption on methyl orange. Therefore, following the optimum process conditions, isotherms, thermodynamics, and kinetics of adsorption of this sample will be examined in the next sections.

**Adsorption Optimum Conditions**

The effective factors of pH, adsorbent amount, contact time, stirring rate, and temperature for evaluating the best adsorption conditions were investigated. The factors were assessed based on the one-factor-at-a-time method, meaning that the values of a factor were changed while the other factors were fixed. Fig. 7 shows diagrams of factors affecting the adsorption process. As shown in Fig. 7a, by increasing the pH from 2 to 10 (methyl orange concentration = 100 mg/L, stirring speed = 200 rpm, contact time = 15 min and adsorbent dosage = 1 g/L), the adsorption amount was initially increased until pH 6 and, then, decreased. It can be referred to as surface change or ionization of methyl orange molecules, in which the adsorbent surface had the highest amount of positive charge at pH = 6 for higher adsorption of methyl orange anion molecules [8]. By increasing the pH of the solution, in addition to reducing the positive surface charges of the adsorbent, the negative ions from the alkaline solution also increase. As these negative ions increase, the competition for adsorption on the adsorbent increases. In other words, MO anion molecules and alkaline-negative ions compete for adsorption on the adsorbent surface with a positive
charge [46]. Other articles have reported the same phenomena that methyl orange adsorption is observed in almost neutral pH [47]. From the results, it can be said that the interaction between the adsorbent and adsorbate molecules is the type of electrostatic forces [48].

The effect of increasing the adsorbent (Fig. 7b) more than 1 g/L showed that the adsorption amount did not increase significantly, which could be due to the interaction of the adsorbent particles with each other and disruption of the proper distribution as well as the increased viscosity of the solution by increasing amount of solid phase [47,3]. In some articles, it has been reported that the amount of adsorption decreases with the increasing amount of adsorbent due to changes in the viscosity of the solution or the limitation of the presence of adsorbate molecules around the adsorbent. [49,50].

The same behavior was observed by increasing the contact time, whereby the adsorption increased to reach equilibrium after about 15 min (Fig. 7c). Due to the saturation of the adsorbent surface with the dye and limitation in mass transfer, the equilibrium would be established and the adsorption value did not change appreciably.

Fig. 7d and Fig. 7e show the effect of changing stirring speed and temperature, respectively. Accordingly, the highest absorption was observed at 200 rpm. It seems that mixing was not performed well at 100 rpm. Also adsorbent did not disperse properly in the solution due to the absorption vortex at 300 rpm. In other words, by creating a vortex, the fluid will move like a rigid object, and as a result, the adsorbent will not mix properly with the adsorbate in the solution [51]. Examination of temperature change showed that, as the temperature increased, the amount of adsorption decreased, indicating that the adsorption was an exothermic process.

According to the studies, the maximum adsorption of methyl orange on MgFe2O4 magnetic adsorbent was obtained at pH = 6, adsorbent content of 1 g/L, the contact time of 15 min, stirring speed of 200 rpm, and temperature of 25°C. Other essential aspects of the adsorption process were investigated under these conditions.

### Isotherms

One of the important points in the adsorption process is the investigation of adsorption isotherms, which allows for investigating the type of interaction between the adsorbent and the adsorbate as well as the final adsorbent capacity. For this purpose, four important isotherms of Langmuir, Freundlich, Temkin, and Dubinin–Radushkevich were investigated for the methyl orange adsorption process on MgFe2O4 surface. The linear equations of these isotherms were evaluated, the results of which are shown in Table 2 and Fig. S2. Fig. S2(a) shows that, at low concentrations of methyl orange (up to 100 mg/L), there was a good agreement between the adsorption data and the Langmuir model ($R^2 = 0.984$ and maximum

### Table 2. Linearized equations of isotherm models for the adsorption of MO on the MgFe2O4 surface.

<table>
<thead>
<tr>
<th>Isotherm Models</th>
<th>Linearized equations</th>
<th>Parameters</th>
</tr>
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<tbody>
<tr>
<td>Langmuir</td>
<td>$C = \frac{1}{K_q q_m} + \left(\frac{1}{q_m}\right) C$</td>
<td>$R^2$, $q_m$ (mg/g), $K_q$ (L/mg)</td>
</tr>
<tr>
<td>Freundlich</td>
<td>$ln q_e = ln K_r + \frac{1}{n} ln C$</td>
<td>$R^2$, $n$, $K_r$ (mg/g), $q_e$ (mg/g)</td>
</tr>
<tr>
<td>Temkin</td>
<td>$q_e = B_1 ln k_1 + B_2 ln C$</td>
<td>$R^2$, $B_1$, $B_2$, $k_1$ (L/mg)</td>
</tr>
<tr>
<td>Dubinin–Radushkevich</td>
<td>$ln q_e = ln q_{m, e} - K_0 e_2^2$</td>
<td>$R^2$, $q_{m, e}$ (mg/g), $K_0$, $E$ (J/mmol) = 1/(2K_0)</td>
</tr>
</tbody>
</table>

$q_m$: the maximum adsorption capacity, $K_q$: Langmuir equilibrium constant, $K_r$ & $n$: Freundlich equation constants, $k_1$: the equilibrium binding constant, $B_i$: the heat of adsorption, $K_0$: the activity coefficient constant related to adsorption energy, $E$: Polanyi potential, $E$: the mean free energy of adsorption.
adsorption capacity = 243.9 mg/g), but with an increase in the initial concentration of adsorbate, the regression coefficient was reduced to 0.8415. The maximum capacity using the Langmuir model obtains 108.7 mg/g (Table 2). The Langmuir isotherm expressed monolayer adsorption on the homogeneous adsorbent surface. So, by coating a layer of adsorbate on the adsorbent surface, the adsorption process reached its maximum value [3].

The high accuracy between adsorption data with the Freundlich model, which expressed the multilayer adsorption of adsorbate on the heterogeneous adsorbent surface [8], can confirm the results (Table 2, Fig. S2b). The results showed that the adsorption process followed the Freundlich theory ($R^2 = 0.949$) in the range of low to high concentrations of methyl orange. The slope of the line ($1/n = 0.75$) in the Freundlich equation expressed the adsorption power of the dye on the heterogeneous adsorbent and its smaller values ($0 < 1/n < 1$) indicated more similarity of the adsorption process to the heterogeneous system and confirmed the suitability of the adsorbent [52]. The maximum adsorption capacity ($q_m$) for the Freundlich model can be calculated from the $q_m = K_f C_0^{1/n}$ formula, in which the initial concentration of MO ($C_0$) is constant against the amount of adsorbent ($K_f$ & $n =$ Freundlich equation constants) [53]. $q_m$ was obtained 181.34 mg/g that revealed Mg-Fe spinel ($\text{MgFe}_2\text{O}_4$) can be an appropriate adsorbent for the dye adsorption process.

Temkin model was also studied on the adsorption data, as presented in Table 2 and Fig. S2c. This theory also explains the interaction between the adsorbate (methyl orange) and the adsorbent ($\text{MgFe}_2\text{O}_4$) as well as its relationship to bond energy. The results demonstrated that the adsorption data were in good agreement with this isotherm model ($R^2 = 0.948$). High consistency of the adsorption data with Temkin theory indicated a strong interaction between the adsorbate and the adsorbent [54].

The last studied isotherm, shown in Table 2 and Fig. S2d, was the Dubinin–Radushkevich model, in which the type of adsorption (chemically or physically), as well as the adsorption mechanism on the surface of heterogeneous porous adsorbents, was presented [55]. As shown in the figure, there was a great deal of agreement between the linearized isotherm equation and the adsorption data ($R^2 = 0.964$) at high concentrations, while less compatibility was observed at low adsorbate concentrations ($R^2 = 0.873$). In other words, against the adsorption process, which performed only on the outer surface or large cavities (macropores) of adsorbent at low concentrations of methyl orange, the adsorption process was performed on small adsorbent pores (mesopores and micropores) at high methyl orange concentration. Based on this theory, the mean free energy of adsorption (E) was 0.029 kJ/mol, which, due to its low content (less than 8 kJ/mol), it can be said that the adsorption of methyl orange on the surface of $\text{MgFe}_2\text{O}_4$ was physical [56].

**Kinetics**

To investigate the mechanism of adsorption and to learn more about the adsorption process, four traditional models (pseudo-first-order, pseudo-second-order models, intraparticle diffusion, and Elovich) used in the adsorption process were assessed. The results are presented in Table 3 (Fig. S3). The adsorption data showed that the adsorption tradition did not follow the pseudo-first-order model. However, the pseudo-second-order model fitted very well with the experimental data and fitted perfectly with the data ($R^2 = 0.9961$), such that the final MO adsorption capacity on the surface of $\text{MgFe}_2\text{O}_4$ was 59.52 mg/g, which was very close to its experimental value ($q_e = 56.54$ mg/g).

Fittings of experimental data based on the intraparticle diffusion model showed that these data are fitted in a multi-linearity manner, and also none of the fitted lines cross the coordinate origin (Intercept is zero). The multi-linearity curves show that the more different stages of the adsorption stage (intraparticle diffusion, film layer diffusion, and interaction between adsorbate and adsorbent surface molecules) may control the rate of the adsorption process [58,59]. According to Table 3, in the first stage, the value of $k_{ci}$ (indicating the rate of absorption) is high and the amount of $C_i$ (showing the diffusion resistance of the film at the adsorbent surface) is low. Therefore, it can be said that in the early stages of the adsorption process, due to the high concentration of adsorbed molecules, the film diffusion resistance is low and the adsorption rate is high (the intraparticle diffusion has probably controlled the rate at this stage). In the next step, with the passage of time and the reduction of methyl orange molecules in the solution and the reduction of the driving force of the mass transfer, the film diffusion resistance increases (the large amount of $C_i$) and the adsorption rate will be decreased (the
film diffusion controls the adsorption rate at this stage).

Inconsistency of the Elovich (R² = 0.7648) model with the experimental data presented that the limitation for the adsorption of dye molecules into the adsorbent surface created by the boundary layer [60].

**Thermodynamics**

The adsorption of MO on the adsorbent was carried out at three different temperatures to investigate the thermodynamics of the process and its results were fitted using the following linear equation, as can be seen in Fig. 8.

\[
\ln \left( \frac{q_e}{C_e} \right) = \frac{\Delta S^o}{R} - \frac{\Delta H^o}{RT} \quad (1)
\]

The fitted equation with the regression coefficient 0.908 was in good agreement with the experimental data. The values of ΔH° and ΔS° were obtained by comparing the above equation and the fitted equation (the constant amount of the gases was R = 8.314 J/mol.K). The results showed negative values for ΔH° (-46.8 kJ/mol) and ΔS° (-0.155 kJ/mol.K), so it can be concluded that the methyl orange adsorption process on the heterogeneous and magnetic surface of MgFe₂O₄ was exothermic. Thus, the increasing temperature would have a negative effect on the adsorption process [61].

The Gibbs free energy (ΔG°) values were also obtained -0.489, 0.236, and 2.640 kJ.mol⁻¹ according to the following equation at 298, 308, and 318 K respectively [62].

\[
\Delta G^o = -RT \ln \left( \frac{q_e}{C_e} \right) \quad (2)
\]

It is shown that the ΔG° is negative at 298 K (optimum temperature) indicating that the MO adsorption process on the MgFe₂O₄ surface is spontaneous at optimum temperature. It is also found that increasing temperature reduces the absorption driving force and the adsorption process will not spontaneously occur at higher temperatures [62]. Given the value of ΔG° (-0.489 kJ/mol⁻¹) at the optimum temperature (298 K) is between 0 and -20 that confirms the low physical interaction between

<table>
<thead>
<tr>
<th>Kinetic Models</th>
<th>Linearized equations</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pseudo-first-order</td>
<td>( \ln(q_e - q_t) = \ln q_e - k_1 t )</td>
<td>R², k₁ (1/min), qₑ (mg/g)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.7014, 0.063, 14.695</td>
</tr>
<tr>
<td>Pseudo-second-order</td>
<td>( t = \frac{1}{k_2 q_e} + \frac{t}{q_e} )</td>
<td>R², k₂ (g/min/mg), qₑ (mg/g)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.9961, 0.0052, 59.534</td>
</tr>
<tr>
<td>Elovich</td>
<td>( q_t = \frac{1}{\beta} \ln(\alpha t) + \frac{1}{\beta} \ln t )</td>
<td>R², β (g/mg), α (mg/mg/min)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.9925, 0.0998, 71.707</td>
</tr>
<tr>
<td>Intraparticle diffusion</td>
<td>( q_t = k_3 t^{0.5} + C )</td>
<td>R², k₃ (g/min¹/mg), C (mg/g)</td>
</tr>
<tr>
<td></td>
<td>Stage 1</td>
<td>R², k₃ (g/min¹/mg), C (mg/g)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>-1.668, 14.565, 53.854</td>
</tr>
<tr>
<td></td>
<td>Stage 2</td>
<td>R², k₃ (g/min¹/mg), C (mg/g)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.9997, 0.2776, 53.854</td>
</tr>
<tr>
<td>Experimental data</td>
<td>qₑ (mg/g)</td>
<td>56.54</td>
</tr>
</tbody>
</table>

*qₑ*: the amount of MO adsorbed on the adsorbent at the equilibrium, *q_t*: the amount of MO adsorbed on the adsorbent at time t, *k₁*: the rate constant of Pseudo-first-order, *k₂*: the rate constant of Pseudo-second order, *β*: the desorption constant during any one experiment, *α*: the initial rate of adsorption, *k₃*: the rate parameter of the intra-particle diffusion control stage, *C*: a constant related to the thickness of the boundary layer.
MO and the adsorbent surfaces. Moreover, it can prove by the value of ΔH° (-46.8 kJ.mol⁻¹) in which the adsorption of MO on the adsorbent is exothermic Physico-chemical adsorption (neither completely physical nor completely chemical) [63]. Therefore, the adsorbate can be removed from the adsorbent surface partly by heating that may be related to reversibility properties.

COMPARING THE RESULTS

Table 4 shows the properties of various adsorbents used to remove dyes from the aqueous medium. In most reported works, the maximum absorption capacity is very different from the results of the present work. In articles that used chitosan microspheres (qₘ=207 mg/g) [46] and functionalized straw (qₘ=325.4 mg/g) [57] as adsorbents, due to the organic nature of the adsorbents and having a high active surface, the amount of adsorption was greater than the magnetic spinel used in the present work (qₑ=181.34 mg/g). The used adsorbent in the present work not only presented a suitable adsorption capacity but also showed suitable magnetic properties that it can easily separate from solution via an external magnet. So this adsorbent can be introduced as a suitable and economical adsorbent for the removal of dyes (such as methyl orange) from water.

CONCLUSIONS

In the present study, two magnetic adsorbents Fe₃O₄ (synthesized by co-precipitation method) and MgFe₂O₄ (synthesized by combustion method) were investigated in the methyl orange adsorption process from the aqueous solution. The results showed that the Fe₃O₄ sample had much higher magnetic strength, which could facilitate the separation of this adsorbent. This sample also had a higher surface area, which is an essential characteristic of the adsorbents. However, the use of the combustion method in the synthesis of the MgFe₂O₄ magnetic spinel resulted in larger pores in this sample, which could compensate for its lower surface area for the simple diffusion of large molecules of MO into the pores and be quickly absorbed. The examination of the samples in the
MO adsorption process confirmed the influence of the pore diameter on the adsorption so that the MgFe₂O₄ showed higher adsorption capacity than Fe₃O₄. Investigation of the adsorption isotherms and kinetics for the MgFe₂O₄ sample proved that the adsorption rate was not controlled by the entry of large MO molecules into the pores as well as by creating a boundary layer on the adsorbent surface. These studies showed that the adsorption step of MO on the MgFe₂O₄ controlled the rate of adsorption. Finally, the thermodynamic study of methyl orange adsorption on the MgFe₂O₄ surface revealed the process was exothermic and spontaneous. At the end of the studies, the MgFe₂O₄ (the maximum adsorption capacity=181.34 mg/g) sample can be suggested for the removal of dyes and water pollutants after further assessment, which will be performed in our future works.

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CONFLICT OF INTEREST

There are no conflicts to declare.

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